## Department of Mathematics \& Statistics Mathematics major and minor

## ASSESSMENT REPORT ACADEMIC YEAR 2021-2022

## LOGISTICS \& PROGRAM LEARNING OUTCOMES

1. Name of program(s) and degree type(s)

The Department of Mathematics and Statistics offers a bachelor's degree in Mathematics and a bachelor's degree in Data Science.
2. Names and contact information of the faculty coordinating the assessment of each program and report

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3. Mathematics Major and Minor Mission Statement

There were no changes to our mission statement since last assessment cycle. Our mission statement remains:

The USF Department of Mathematics \& Statistics seeks to deliver a quality mathematics education to our majors and minors, inspiring them to appreciate, understand, and engage with clear and rigorous thinking, both in abstract and concrete settings.
4. Mathematics Major and Minor Program Learning Outcomes

There were no changes made to our PLOs.

1. Differentiate and integrate functions of one and several variables;
2. Use differentiation and integration to solve problems in mathematics and other disciplines;
3. Solve and understand linear systems;
4. Give direct proofs, proofs by contradiction, and proofs by induction; formulate definitions and construct counterexamples;
5. Read mathematics without supervision; write mathematics with correct style, including typesetting;
6. Apply mathematics to problems in other disciplines; and
7. Use technology to solve mathematical problems.

## Curricular Map

## Curriculum Map for Program Learning Outcomes and Math Courses

|  | PLO - 1 | PLO - 2 | PLO - 3 | PLO - 4 | PLO - 5 | PLO - 6 | PLO - 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Math 109 | $\checkmark$ | $\checkmark$ |  |  | $\checkmark$ |  |  |
| Math 110 | $\checkmark$ | $\checkmark$ |  |  | $\checkmark$ |  |  |
| Math 211 | $\checkmark$ | $\checkmark$ |  |  | $\checkmark$ |  |  |
| Math 230 |  |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| Math 235 |  |  |  | $\checkmark$ | $\checkmark$ |  |  |
| Math 310 |  |  |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| Math 314 |  |  |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| Math 340 | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  | $\checkmark$ | $\checkmark$ |
| Math 345 |  |  | $\checkmark$ |  |  | $\checkmark$ | $\checkmark$ |
| Math 350 |  |  |  |  | $\checkmark$ | $\checkmark$ |  |
| Math 355 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  |  |
| Math 367 |  |  |  | $\checkmark$ | $\checkmark$ |  |  |
| Math 370 | $\checkmark$ | $\checkmark$ |  |  |  | $\checkmark$ |  |
| Math 371 | $\checkmark$ | $\checkmark$ |  |  |  | $\checkmark$ |  |
| Math 372 |  |  |  |  |  | $\checkmark$ | $\checkmark$ |
| Math 373 |  |  |  |  |  | $\checkmark$ | $\checkmark$ |
| Math 375 |  |  | $\checkmark$ |  |  | $\checkmark$ | $\checkmark$ |
| Math 380 |  |  |  | $\checkmark$ | $\checkmark$ |  |  |
| Math 422 |  |  |  | $\checkmark$ | $\checkmark$ |  |  |
| Math 435 |  |  |  | $\checkmark$ | $\checkmark$ |  |  |
| Math 453 | $\checkmark$ |  |  | $\checkmark$ | $\checkmark$ |  |  |
| Math 482 |  |  |  | $\checkmark$ | $\checkmark$ |  |  |
| Math 485 |  |  |  | $\checkmark$ | $\checkmark$ |  |  |

## 5. Assessment schedule between APRs

We have assessed PLOs 1, 2, 3, 4, 5, and 6 each year since our last Academic Program Review in 2017 through a standardized exit exam. We will continue this plan until it proves to be an unsuccessful measure of assessment.

## METHODOLOGY

## 6. Description of the methodology used to assess the PLO(s)

To assess the aforementioned Program Learning Outcomes, our graduating math majors took the ETS Major Field Test for Mathematics in April 2022. This exam is written by the Educational Testing Service, the same organization that writes the GRE and TOEFL. In the past year (June 2021 - June 2022) this exam was taken by graduating math majors at different institutions all across the United States. The total number of examinees is usually around 1,000.

The exam has 50 multiple choice questions and covers topics most commonly offered as part of an undergraduate mathematics curriculum.

The content breakdown of the exam is as follows:

- Calculus (about 30\%)

Both single-variable and multivariable calculus.

- Linear \& Abstract Algebra (about 30\%)

Matrices, linear transformations, eigenvalues, eigenvectors, vector spaces, systems of linear equations, elementary group/ring/field theory, elementary topics from number theory.

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- Additional Topics (about 40\%)

Complex analysis, differential equations, discrete mathematics (including graph theory and combinatorics), foundations (including logic, proofs, sets, functions and relations), geometry, point-set topology, probability and statistics, and real analysis.

The exam questions are at three cognitive levels:

- Routine (about 55\%)

These questions cover definitions, questions with no more than a two-step reasoning process, or questions that require a standard technique that is practiced extensively in math courses at most institutions.

- Non-routine (about 25\%)

Includes questions that require an idea that is considered insightful, questions that require several steps of reasoning, and questions that require either the use of several definitions or a new definition that the student would not be expected to know. Some questions may require bringing techniques from two or more areas to bear on one problem.

- Applied (about 20\%)

This includes, for example, questions that are cast in real-world settings.

The relationship between this exam and our Program Learning Outcomes is as follows:

- $30 \%$ percent of the exam problems cover calculus knowledge, which corresponds to Program Learning Outcomes 1 and 2.
- $30 \%$ of the exam problems cover algebra knowledge, which corresponds to Program Learning Outcomes 3 and 4.
- $25 \%$ of the exam problems are classified as non-routine, requiring several steps of reasoning or a new definition that the student would not be expected to know, which corresponds to Program Learning Outcomes 4 and 5.
- $20 \%$ of the exam problems are classified as applied, requiring the student to apply math to real-world settings. This corresponds to Program Learning Outcome 6.


## RESULTS \& MAJOR FINDINGS

## 7. Description of results and significant findings from the data or assessment process

This year we had 4 mathematics majors who took the ETS Major Field Test for Mathematics, known in our department as the Mathematics Senior Exit Exam. There was a wide range of scores: between $17^{\text {th }}$ and $93^{\text {th }}$ percentiles when compared to all test takers from undergraduate institutions across the nation. Below is a chart detailing the outcome for each student.

| Student | Score out of 200 | Percentile |
| :---: | :---: | :---: |
| 1 | 189 | $93^{\text {rd }}$ |
| 2 | 156 | $53^{\text {rd }}$ |
| 3 | 153 | $45^{\text {th }}$ |
| 4 | 141 | $17^{\text {th }}$ |

Table 1. USF Graduating Math major scores on the 2022 ETS Major Field Test for Mathematics. The scale range for the total score is $120-200$.

Data collected by ETS from senior test takers from domestic institutions from September 2018 through June 2022 is summarized in the following tables. Table 2 compares USF scores to individual and institutional nationwide data. Table 3 is a breakdown of how our students compare to other test takers according to the question type.

|  | Number | Mean <br> score | Median | Standard <br> Deviation |
| :--- | :--- | :--- | :--- | :--- |
| Nationwide individual aggregate | 5963 | 157.5 | 156 | 17.9 |
| 2018 to 2022 |  |  | 154.5 | 18 |
| USF 2022 | 4 | 160 | 163 | 12 |
| USF 2021 | 8 | 160 | 175.5 | 20 |
| USF 2019 | 6 | 172.8 | 153 | 22 |
| USF 2018 | 13 | 157 | 22 |  |
| USF 2017 | 11 | 159 | 158 | 20 |
| USF 2016 | 12 | 161 | 154.5 |  |

Table 2. USF Graduating Math major scores on the 2021 ETS Major Field Test for Mathematics as compared to previous years and nationwide data.

|  | Calculus | Algebra |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Questions | Questions | Applied <br> Questions | Routine <br> Questions | Non-routine <br> Questions |  |
| Nationwide Aggregate <br> 2017 to 2021 | 31.4 | 33.9 | 35.5 | 33.7 | 26.4 |
| USF 2021 | 41 | 32 | 44 | 36 | 27 |
| USF 2019 | 48 | 48 | 55 | 52 | 28 |
| USF 2018 | 27 | 35 | 33 | 29 | 38 |
| USF 2017 | 30 | 35 | 38 | 32 | 30 |
| USF 2016 | 30 | 45 | 33 | 38 | 29 |

Table 3. A breakdown of performance on the ETS Major Field Test in Mathematics by question type. Numbers in table represent the mean percent correct for each question type.

The ETS does not make available data about individual topics for cohorts of size smaller than 5, so the 2022 cohort information is not included here. We did not administer the exit exam during 2020 due to the pandemic. The students who took the exam in 2022 performed similarly to our students in the past.

## Feedback from previous year's report

We had a rather abrupt change in department leadership in the last weeks of the Spring 2022 semester. We hope to work on implementing some of the ideas in earlier and forthcoming feedback reports once the dust settles. We did start doing an exit interview a few years ago, and I'm not sure why information gathered in those didn't appear in last year's report. I do know that our previous chair did not administer it last year.

Thanks for all your work, Jack, et al. :)
Jennifer

